# ACTIVATION ENERGY OF Se<sub>2</sub>Ge<sub>0.2</sub>Sb<sub>0.8</sub> CHALCOGENIDE GLASS BY DIFFERENTIAL SCANNING CALORIMETRY

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## Abstract

Results of differential scanning calorimetry (DSC) at different heating rates on Se<sub>2</sub>Ge<sub>0.2</sub>Sb<sub>0.8</sub> chalcogenide glass are reported and discussed. As the heating rate ( $\alpha$ ) changed, also the glass transition temperature ( $T_g$ ) and onset temperature of crystallization ( $T_c$ ) changed. As the value of the transition activation energy  $E_t$  changed, the crystallization fraction ( $\chi$ ), heat flow ( $\Delta q$ ) and the crystallization peak temperature ( $T_p$ ) also changed. The value of the effective activation energy of crystallization  $E_c$  was calculated by means of six different methods. The Se<sub>2</sub>Ge<sub>0.2</sub>Sb<sub>0.8</sub> chalcogenide glass has two crystallization mechanisms, a one-dimensional and an other surface crystallization growth. The average value of  $E_t$  for Se<sub>2</sub>Ge<sub>0.2</sub>Sb<sub>0.8</sub> is equal to 194.95± 3.9 kJ·mol<sup>-1</sup> and the average value of  $E_c$  is equal to 164±3.3 kJ·mol<sup>-1</sup>.

Keywords: activation energy, chalcogenide glass, DSC

## Introduction

The physical properties of chalcogenide glasses have lately received a great deal of attention in many technical and scientific applications. The changes in these properties have been used to follow the phase transition from the amorphous to the crystalline state. The activation energy was used as a parameter for observing the steps of the crystallization process with sufficient accuracy [1]. In the present work crystallization studies were carried out under non-isothermal conditions with samples heated at various uniform rates. The glass transition temperature  $T_g$  and both the onset  $(T_c)$  and peak temperature  $(T_p)$  of crystallization are dependent on the heating rate  $(\alpha)$ . The glass transition activation energy  $E_t$ , and crystallization activation energy  $E_c$  were evaluated.

## Experimental

The investigated samples of  $Se_2Ge_{0.2}Sb_{0.8}$  were prepared from appropriate amounts of high purity (99.999%) chemicals put in a quartz glass ampoule

(12 mm diameter) and sealed in a vacuum of  $10^{-4}$  torr then heated in a rotary furnace at 950°C for 24 h. The melt was quenched in water at 0°C [2].

The thermal behavior of the product was investigated with a Shimadzu 50 differential scanning calorimeter. The temperature and energy calibrations of the instrument were performed using the well known melting temperature and melting enthalpy of high-purity indium metal. The calorimetric sensitivity is 10 W (0.008 mJ/s) and the temperature precision is  $\pm 0.1$  K.

X-ray studies of  $Se_2Ge_{0.2}Sb_{0.8}$  powder were performed with a Philips type 1710 diffractometer. The patterns were run with Cu as target and Ni as filter ( $\lambda=0.15417$  nm), at 40 kV and 30 mA, at a scanning speed of 3.6 deg·min<sup>-1</sup>.

The crystallization curves were recorded while the temperature of the sample was increased at a uniform rate. 10 mg of sample in powder form was placed in a standard aluminium cell and scanned over a temperature range from room temperature to 400°C at uniform heating rates ranging from 2 to 50 deg min<sup>-1</sup> in vacuum (10<sup>-2</sup> Torr). The parameters  $T_g$ ,  $T_c$ ,  $T_p$ ,  $\chi$ ,  $\Delta q$  were evaluated by the software of Shimadzu. Figure 1 shows the curve of the sample recorded at a heating rate of 30 deg min<sup>-1</sup>.

#### **Results and discussion**

A typical DSC trace of the prepared  $Se_2Ge_{0.2}Sb_{0.8}$  glass obtained at a heating rate of 30 deg·min<sup>-1</sup>, is shown in Fig. 1. Three characteristic phenomena are



Fig. 1 Typical DSC trances at a heating rate of 30 deg·min<sup>-1</sup> for Se<sub>2</sub>Ge<sub>0.2</sub>Sb<sub>0.8</sub> chalcogenide glass

observed in the studied temperature range. The first one  $T_g$  corresponds to the glass transition temperature, the second one  $T_c$  corresponds to the onset temperature of crystallization, and the last characteristic temperature  $T_p$  is the peak temperature of crystallization of Se<sub>2</sub>Ge<sub>0.2</sub>Sb<sub>0.8</sub> glass. The X-ray diffractogram also indicates that the as-prepared sample is amorphous (Fig. 2).



Fig. 2 The X-ray diffractograms of Se<sub>2</sub>Ge<sub>0.2</sub>Sb<sub>0.8</sub>

From the Jonson-Mehl-Avrami equation [3], the activation energy of crystallization  $(E_c)$  is:

$$E_c = (E_{\rm N} + mE_{\rm c})/n \tag{1}$$

where *n* is an integer of half integer which depends on the mechanism of growth and the dimensions of the crystal.  $E_N$  and  $E_G$  are the effective activation energies for nucleation and growth, respectively, n=m for  $I_v=0$  [4] and n=m+1 for  $I_v\neq 0$  [3], since  $I_v$  is the nucleation energy.

If  $E_N$  is negligible over the temperature range of concern in the thermoanalytical study [3], then

$$E_{\rm c} \cong (m/n) E_{\rm G} \tag{2}$$

Thus, the activation energy of growth  $(E_G)$  is

$$E_{\rm G} \cong (nE_{\rm c} \ /m) \tag{3}$$

There are six different methods for the determination of the effective activation energy of the crystallization process [5, 6]. Two methods Piloyan-Borchardt, and Coats-Redfern-Šesták were used for evaluation of  $E_G$  from one DSC trace, and four other methods Augis-Bennet, Takhor, Kissinger and Ozawa-Chen were used for the determination of  $E_G$  from different traces obtained at different heating rates. The method of Piloyan-Borchardt [7, 8] determines the variation of  $\Delta q$  (the heat flow difference between the sample and reference material) with temperature at constant heating rate. In this method the following equation is used:

$$\ln \left[T \Delta q / F(\chi)\right] = \left(-E_{\rm c} / RT\right) + \text{const.} \tag{4}$$

where R is gas constant,  $F(\chi) = (1-\chi) \left[-\ln(1-\chi)\right]^{\{(n-1)/n\}}$ .

The Coats-Redfern-Šesták method [9] determines the influence of temperature on the crystallization fraction  $(\chi)$  for one heating rate. In this method the following equation is used:

$$\ln[-\ln(1-\chi)/T^{2n}] = (-nE_c/RT) + \text{const.}$$
 (5)

The methods of Augis-Bennett [10] and Takhor [11] use the relationship

$$\ln[\alpha/(T_{\rm p} - T_{\rm o})] = (-E_{\rm c}/RT_{\rm p}) + \text{const.}$$
(6)

where  $T_{o}$  is the initial temperature, and if  $T_{p} >> T_{o}$ , Eq. 6 becomes

$$\ln(\alpha/T_{\rm p}) = (-E_{\rm c}/RT_{\rm p}) + \text{const.}$$
(7)

Kissinger's method [12, 13] is commonly used in analyzing crystallization data in DSC and DTA systems. This method applies the following equation for the determination of the activation energy of crystallization.

$$\ln(\alpha/T_{\rm p}) = (-E_{\rm c} / RT_{\rm p}) + \text{const.}$$
(8)

The last method, that of Ozawa [14] and Chen [15], employs the relationship:

$$\ln(\alpha/T) = (-nE_c /RT) + \text{const.}$$
(9)

at constant volume fraction ( $\chi$ ).

#### Glass transition

The dependence of the glass transition temperature on the heating rate ( $\alpha$ ) was found to follow the formula [15]

$$\ln(\alpha/T_g^2) = (-E_t / RT_g) + \text{const.}$$
(10)

where  $E_t$  is the activation energy of glass transition. If the variation of  $T_g$  is small at different rates ( $\alpha$ ) Eq. 10 becomes

$$\ln(\alpha) = (-E_t / RT_g) + \text{const.}$$
(11)

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Fig.3 (a) Relationship between  $\ln(\alpha/T_g^2)$  and  $1000/T_g$  of Se<sub>2</sub>Ge<sub>0.2</sub>Sb<sub>0.8</sub> glass sample. (b) relationship between  $\ln(\alpha)$  with  $1000/T_g$  of Se<sub>2</sub>Ge<sub>0.2</sub>Sb<sub>0.8</sub> glass sample



Fig. 4 Relationship between  $\ln(\alpha/T_c^2)$  and  $1000/T_c$  for Se<sub>2</sub>Ge<sub>0.2</sub>Sb<sub>0.8</sub> chalcogenide glass

To study and determine the activation energy of glass transition  $E_t$  by using two different methods, in the first one the glass transition temperature  $T_g$  and in the second one the onset temperature of crystallization,  $T_c$  was used.

In the first method relationships (10) and (11) were used. Figure 3 curve (a) shows the correlation between  $\ln(\alpha/T_g^2)$  and  $1/T_g$ , and Fig. 3 curve (b) shows the relationship between  $\ln(\alpha)$  and  $1/T_g$ . The values of  $E_t$  deduced were found to be  $191.73\pm4.41$  kJ·mol<sup>-1</sup> and  $199.18\pm4.38$  kJ·mol<sup>-1</sup>, respectively.

In the second method Kissinger's formula [12] was used which had been applied originally to crystallization studies. The dependence of  $T_c$  on  $\alpha$  is given by

$$\ln(\alpha/T_c^2) + \text{const.} = -E_t / RT_c$$
(12)

A plot of  $\ln(\alpha/T_c^2)$  vs.  $1/T_c$  for the Se<sub>2</sub>Ge<sub>0.2</sub>Sb<sub>0.8</sub> chalcogenide glass is shown in Fig. 4. The value of  $E_t$  was found to be 198.16±3.96 kJ·mol<sup>-1</sup>.

#### Crystallization process

Before evaluation of the effective activation energy of crystallization  $E_c$ , the Ozawa method deduces the order of the crystallization reaction (*n*) using Eq. (5).



Fig. 5 Relationship between  $\ln[-\ln(1-\chi)]$  and  $\ln(\alpha)$  at temperature of 510 K and 521 K for Se<sub>2</sub>Ge<sub>0.2</sub>Sb<sub>0.8</sub> glass

$$d\{ \ln[-\ln(1-\chi)] \} / d\{ \ln(\alpha) \} = -n$$

where  $\alpha$  is the heating rate.

On this basis,  $\ln[-\ln(1-\chi)]$  is plotted vs.  $\ln \alpha$ , at the same temperature. The value of *n* for different heating rates was calculated. Figure 5 shows the relationships at temperatures of 510 and 521 K.

The average slope was 1.8, which means that n=2 and m=1, and the crystallization occurs by two different mechanisms, surface nucleation and bulk nucleation [one-dimensional growth].

The activation energy of crystallization was calculated by means of the Piloyan-Borchardt method form Eq. (4) by plotting  $\ln[T\Delta q/F(\chi)]$  vs. 1/T. Figure 6 shows this relationship at a rate of 10 deg·min<sup>-1</sup>, the slope being  $-E_c/RT$ , thus  $E_c = 142.27$  kJ·mol<sup>-1</sup>.



Fig. 6 Relationship between  $\ln[T\Delta q/F(\chi)]$  and (1000/T) at a heating rate of 10 deg min<sup>-1</sup> for Se<sub>2</sub>Ge<sub>0.2</sub>Sb<sub>0.8</sub> glass

 $E_c$  was evaluated by means of the Coats-Redfern-Šesták method, using Eq. (5), by plotting  $\ln[-\ln(1-\chi)/T^4]$  vs. 1/T, at different heating rates (n=2). Figure 7 shows the average slope to be equal to  $nE_c/R$ , thus  $E_c = 163.77 + 23.4 \text{ kJ} \cdot \text{mol}^{-1}$ .

The activation energy of crystallization was determined by means of the methods of Augis-Bennett and Takhor using Eq. (7), since  $T \ll T$  in this work.



Fig. 7 Relationship between  $\ln[-\ln(1-\chi)/T^4]$  and (1000/T) for Se<sub>2</sub>Ge<sub>0.2</sub>Sb<sub>0.8</sub> glass



Fig. 8 (a) variation of  $\ln[\alpha/T_p)\min^{-1}$  and  $1000/T_p$ , (b) variation of  $\ln[\alpha/T_p^2(\min^{-1} \cdot \mathbf{K}^{-1})]$  with  $1000/T_p$  for Se<sub>2</sub>Ge<sub>0.2</sub>Sb<sub>0.8</sub> glass



Fig. 9 Relationship between  $\ln(\alpha/T)$  and 1000/T at various volume fractions ( $\chi=0.3, 0.4, 0.5, 0.6$ ) for Se<sub>2</sub>Ge<sub>0.2</sub>Sb<sub>0.8</sub> glass

The relation between  $\ln(a/T_p)$  and vs.  $1/T_p$  is shown by curve (a) in Fig. 8  $E_c$  was evaluated from the slope as  $E_c = 176.93 \text{ kJ} \cdot \text{mol}^{-1}$ .

In Kissinger's method Eq. (8) was used  $\ln(\alpha/T_p^2)$  was plotted vs.  $1/T_p$ , as shown by curve (b) in Fig. 8. From the slope  $E_c$  was calculated as  $E_c = 172.62 \text{ kJ} \cdot \text{mol}^{-1}$ .

In the last method, that of Ozawa and Chen, Eq. (9) was used. The relationship between  $\ln(\alpha/T)$  vs. 1/T for different volume fractions ( $\chi = 0.3$ , 0.4, 0.5, 0.6) is shown in Fig. 9. From the slope, the average value of the activation energy of crystallization was calculated ( $E_c = 168.65 \text{ kJ} \cdot \text{mol}^{-1}$ ). Table 1 shows  $E_c$ and  $E_G$  calculated by means of different methods.

Methods used	$E_c$ / kJ·mol <sup>-1</sup>	$E_{\rm G}$ / kJ·mol <sup>-1</sup>
Piloyan-Borchardt	142.27	284.54
Coats-Redfern-Šesták	163.77	327.54
Augis-Bennett & Takhor	176.93	353.80
Kissinger	172.62	345.24
Ozawa-Chen	168.65	337.30

Table	1
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## Conclusion

The mean value of the effective activation energy of crystallization  $E_c$  is equal to  $164\pm3.3 \text{ kJ}\cdot\text{mol}^{-1}$ , and the average value of the effective activation energy of crystal growth ( $E_G$ ) for Se<sub>2</sub>Ge<sub>0.2</sub>Sb<sub>0.8</sub> glass obtained by means of six different methods under non-isothermal conditions is  $328\pm6.6 \text{ kJ}\cdot\text{mol}^{-1}$ , and the average value of the transition activation energy  $E_t$  is  $194\pm3.9 \text{ kJ}\cdot\text{mol}^{-1}$ . The crystallization mechanism for Se<sub>2</sub>Ge<sub>0.2</sub>Sb<sub>0.8</sub> glass is a two-dimensional growth.

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